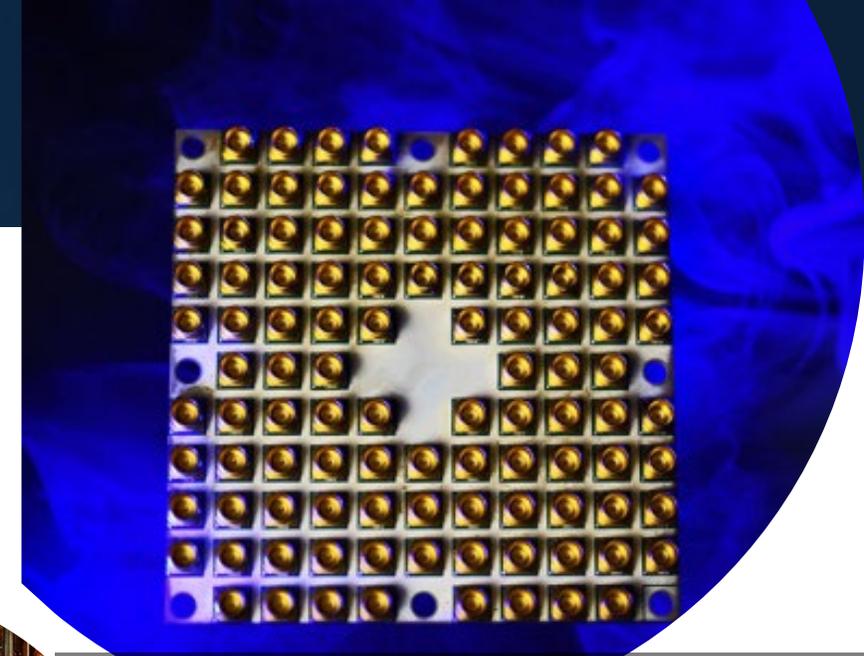


# Cryptography in a Post-Quantum World

Dustin Moody

# Quantum Computers

- Exploit quantum mechanics to process information
- "Qubits" instead of bits
- Potential to vastly increase computational power beyond classical computing limit
- Limitations:
  - When a measurement is made on quantum system, superposition collapses
  - Only good at certain problems
  - Quantum states are very fragile and must be extremely well isolated



Intel's 49-qubit chip "Tangle-Lake"



IBM's 50-qubit quantum computer



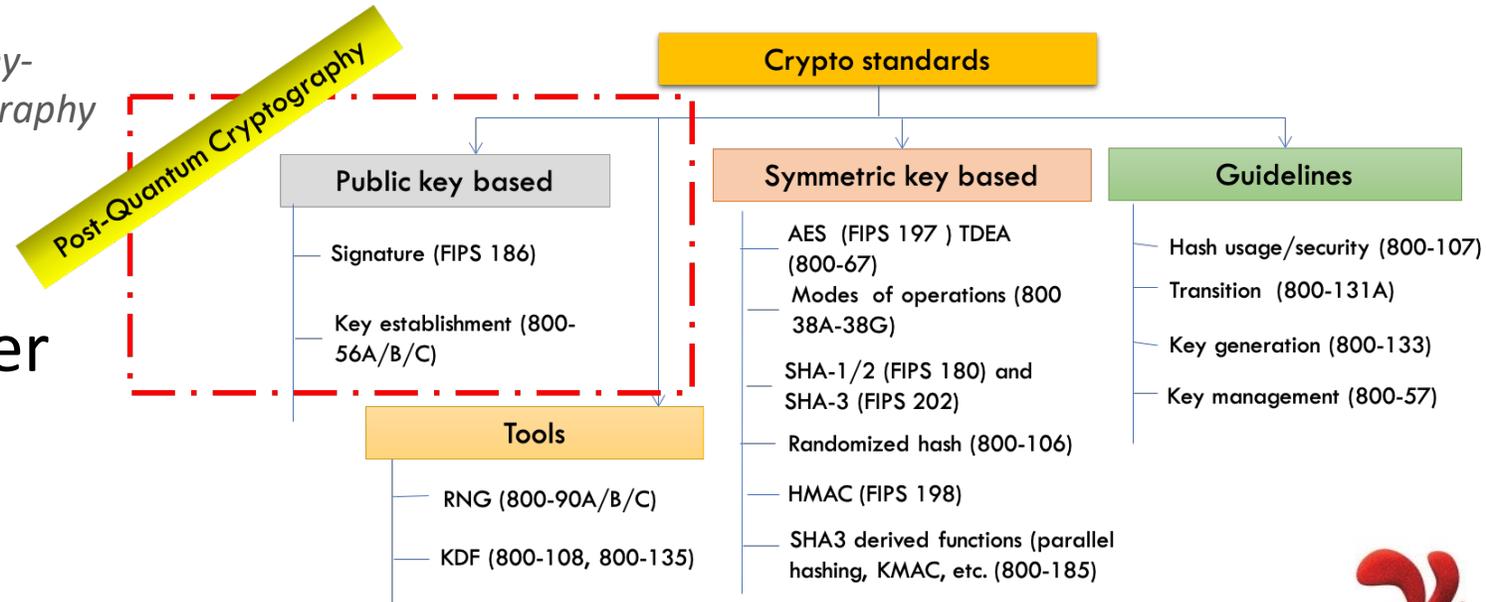
Google's 72-qubit chip "Bristlecone"

# The Quantum Threat

- NIST public-key crypto standards
  - **SP 800-56A**: *Recommendation for Pair-Wise Key-Establishment Schemes Using Discrete Logarithm Cryptography*
  - **SP 800-56B**: *Recommendation for Pair-Wise Key-Establishment Using Integer Factorization Cryptography*
  - **FIPS 186**: *The Digital Signature Standard*

vulnerable to attacks from a (large-scale) quantum computer

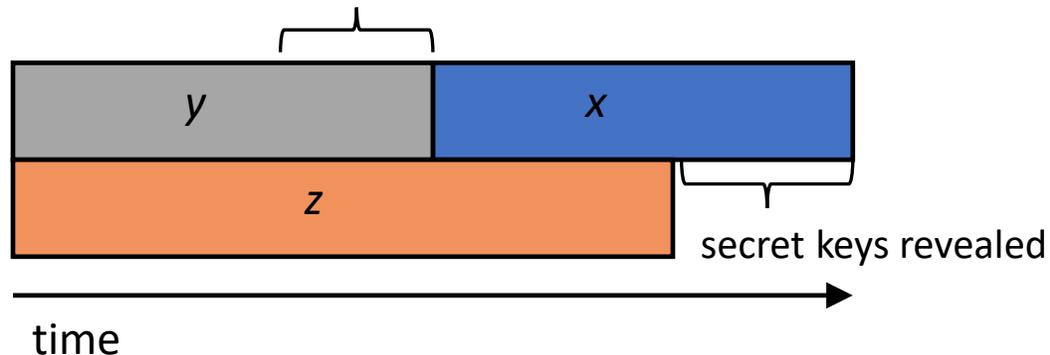
- Shor’s algorithm would break RSA, ECDSA, (EC)DH, DSA
- Symmetric-key crypto standards would also be affected, but less dramatically



- Post-Quantum Cryptography (PQC)
  - Cryptosystems which run on classical computers, and are believed to be resistant to attacks from both classical and quantum computers
- How soon do we need to worry?

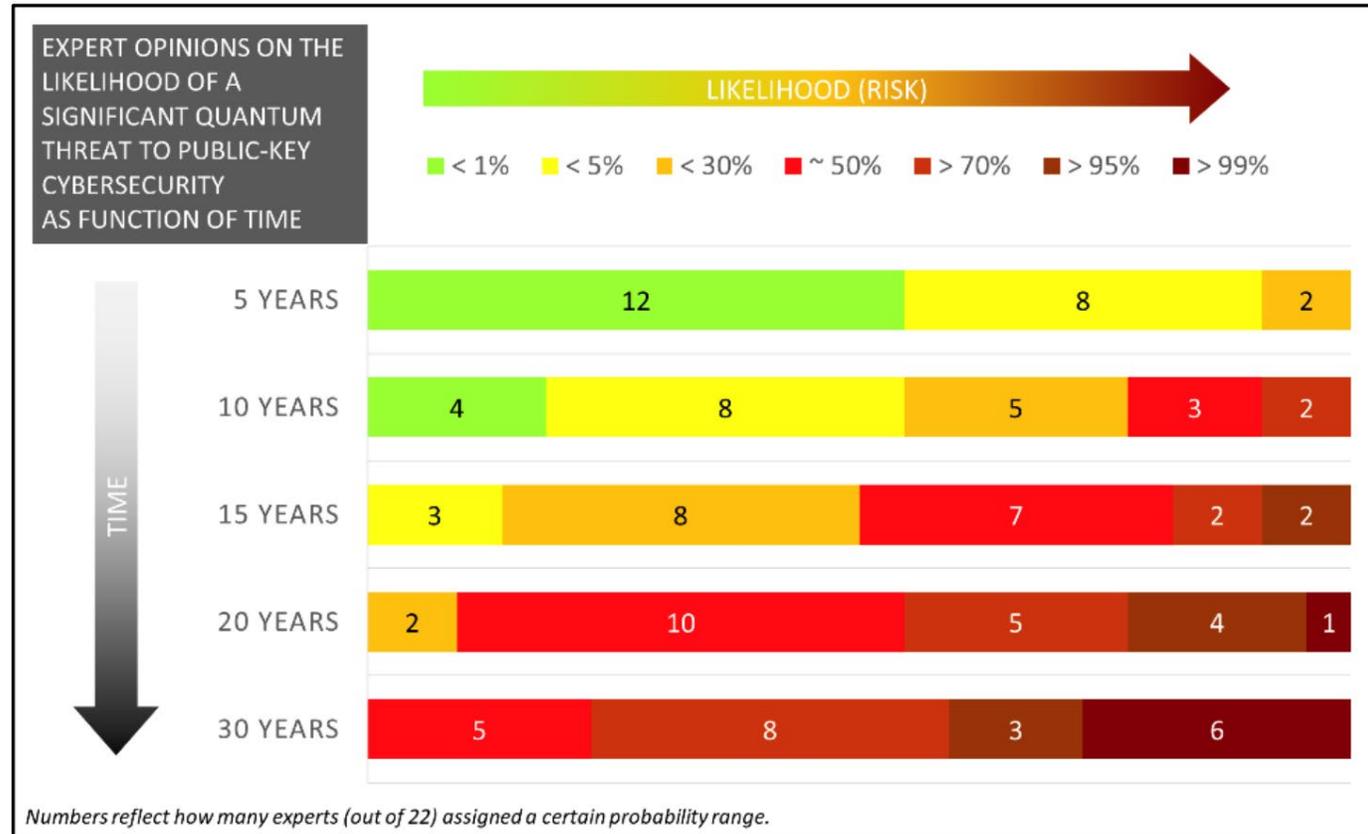
Theorem (Mosca): If  $x + y > z$ , then worry

What do we do here??



- $x$  – time of maintaining data security
- $y$  – time for PQC standardization and adoption
- $z$  – time for quantum computer to be developed

# When will a Quantum Computer be Built?



Source: M. Mosca, M. Piani, Quantum Threat Timeline Report, Oct 2019  
available at: <https://globalriskinstitute.org/publications/quantum-threat-timeline/>

# Quantum Cryptography aka QKD

Using quantum technology to build cryptosystems

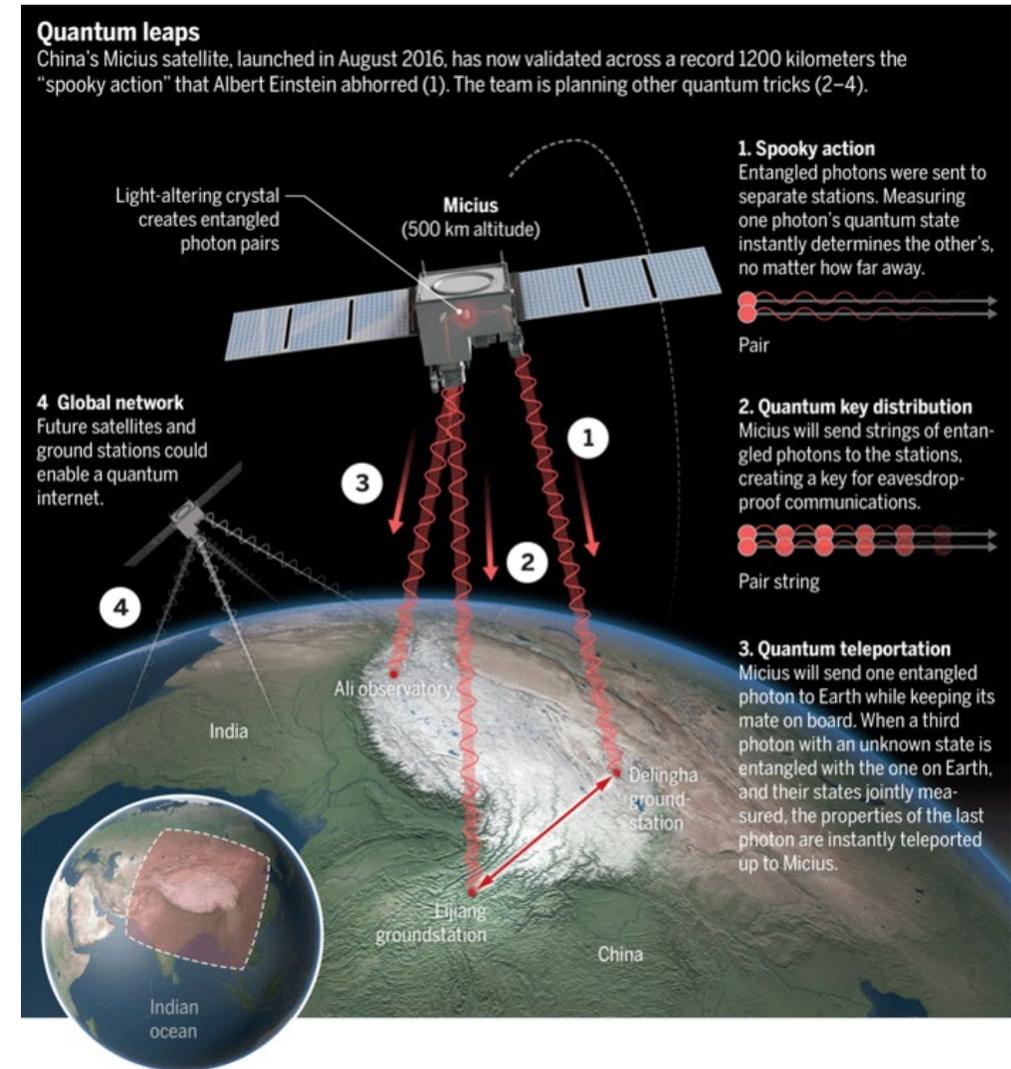
- Theoretically unconditional security guaranteed by the laws of physics

## Limitations

- Can do encryption, but not authentication
- Quantum networks not very scalable
- Expensive and needs special hardware

Lots of money being spent on “quantum”

This is NOT our focus



# NIST PQC Milestones and Timelines



## 2016

Determined criteria and requirements, published [NISTIR 8105](#)

Announced call for proposals

## 2017

Received 82 submissions

Announced 69 1<sup>st</sup> round candidates

## 2018

Held the 1<sup>st</sup> NIST PQC standardization Conference

## 2019

Announced 26 2<sup>nd</sup> round candidates, [NISTIR 8240](#)

Held the 2<sup>nd</sup> NIST PQC Standardization Conference



## 2020

Announced 3rd round 7 finalists and 8 alternate candidates. [NISTIR 8309](#)

## 2021

Hold the 3<sup>rd</sup> NIST PQC Standardization Conference

## 2022-2023

Release draft standards and call for public comments



# Evaluation Criteria

**Security** – against both classical and quantum attacks

| Level | Security Description  |
|-------|---|
| I     | At least as hard to break as AES128 (exhaustive key search) |
| II    | At least as hard to break as SHA256 (collision search)      |
| III   | At least as hard to break as AES192 (exhaustive key search) |
| IV    | At least as hard to break as SHA384 (collision search)      |
| V     | At least as hard to break as AES256 (exhaustive key search) |

NIST asked submitters to focus on levels 1,2, and 3. (Levels 4 and 5 are for very high security)

**Performance** – measured on various classical platforms

**Other properties:** Drop-in replacements, Perfect forward secrecy, Resistance to side-channel attacks, Simplicity and flexibility, Misuse resistance, etc.

# A Worldwide Effort



25 Countries

16 States

6 Continents

# The 1<sup>st</sup> Round

- A lot of schemes quickly attacked!
- Many similar schemes (esp. lattice KEMs)
- 1<sup>st</sup> NIST PQC Standardization workshop
- Over 300 "official comments" and 900 posts on the pqc-forum
- Research and performance numbers
- After a year: 26 schemes move on



|                                   | Signatures | KEM/Encryption | Overall   |
|-----------------------------------|------------|----------------|-----------|
| Lattice-based                     | 5          | 21             | 26        |
| Code-based                        | 2          | 17             | 19        |
| Multi-variate                     | 7          | 2              | 9         |
| Stateless Hash or Symmetric based | 3          |                | 3         |
| Other                             | 2          | 5              | 7         |
| <b>Total</b>                      | <b>19</b>  | <b>45</b>      | <b>64</b> |

# The 2nd Round

- 4 merged submissions
- Maintained diversity of algorithms
- Cryptanalysis continues
  - LAC, LEDAcrypt, RQC, Rollo, MQDSS, qTESLA, LUOV all broken
- 2<sup>nd</sup> NIST PQC Standardization workshop
- More benchmarking and real world experiments
- After 18 months: 15 submissions move on



|                                   | Signatures | KEM/Encryption | Overall   |
|-----------------------------------|------------|----------------|-----------|
| Lattice-based                     | 3          | 9              | 12        |
| Code-based                        |            | 7              | 7         |
| Multi-variate                     | 4          |                | 4         |
| Stateless Hash or Symmetric based | 2          |                | 2         |
| Isogeny                           |            | 1              | 1         |
| <b>Total</b>                      | <b>10</b>  | <b>16</b>      | <b>26</b> |

# Challenges and Considerations in Selecting Algorithms



## Security

- Security levels offered
- (confidence in) security proof
- Any attacks
- Classical/quantum complexity

## Performance

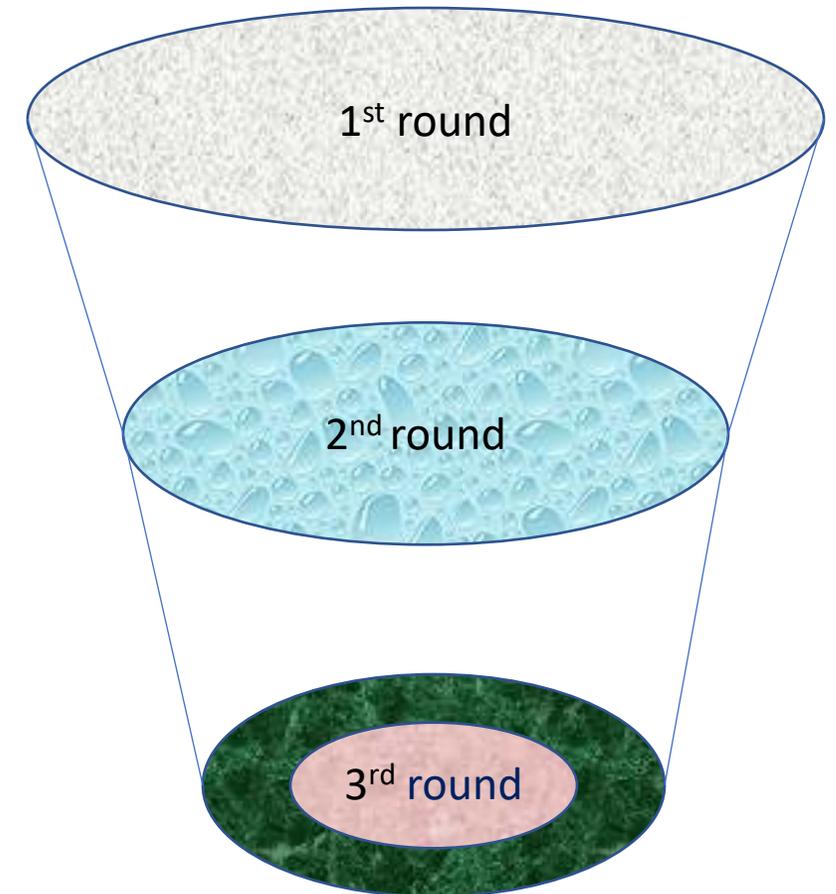
- Size of parameters
- Speed of KeyGen, Enc/Dec, Sign/Verify
- Decryption failures

## Algorithm and implementation characteristics

- IP issues
- Side channel resistance
- Simplicity and clarity of documentation
- Flexible

## Other

- Round 2 changes
- Official comments/pqc-forum discussion
- Papers published/presented



# The 3<sup>rd</sup> Round Finalists and Alternates

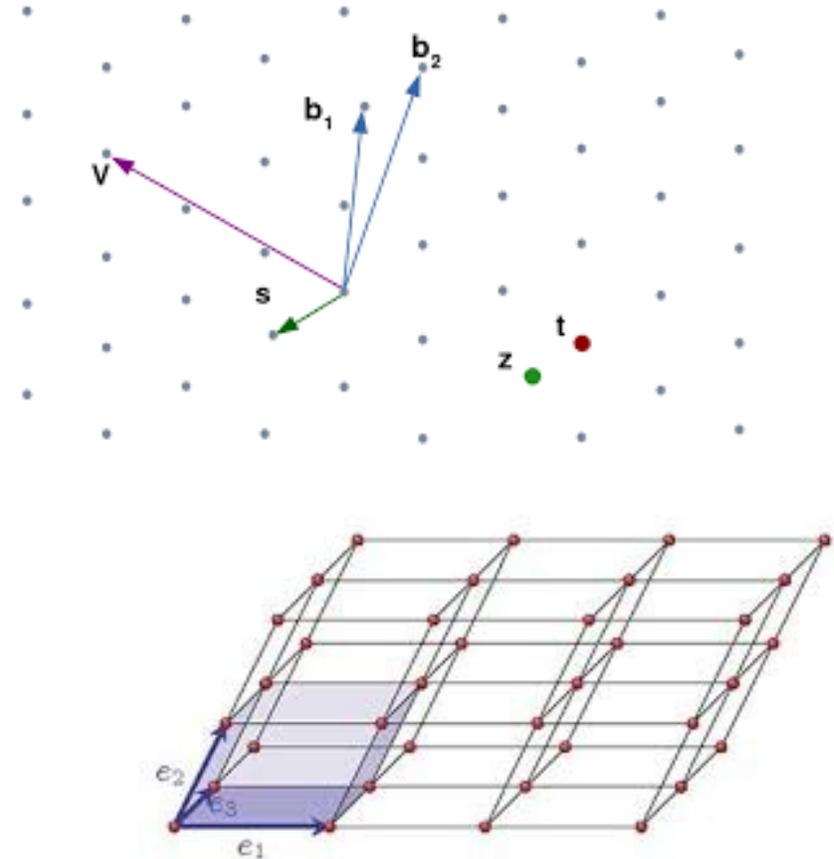


- NIST selected 7 **Finalists** and 8 **Alternates**
  - **Finalists**: most promising algorithms we expect to be ready for standardization at end of 3<sup>rd</sup> round
  - **Alternates**: candidates for potential standardization, most likely after another (4th) round
- KEM finalists: Kyber, NTRU, SABER, Classic McEliece
- Signature finalists: Dilithium, Falcon, Rainbow
- KEM alternates: Bike, FrodoKEM, HQC, NTRUprime, SIKE
- Signature alternates: GeMSS, Picnic, Sphincs+

|                                   | Signatures |   | KEM/Encryption |   | Overall |   |
|-----------------------------------|------------|---|----------------|---|---------|---|
| Lattice-based                     | 2          |   | 3              | 2 | 5       | 2 |
| Code-based                        |            |   | 1              | 2 | 1       | 2 |
| Multi-variate                     | 1          | 1 |                |   | 1       | 1 |
| Stateless Hash or Symmetric based |            | 2 |                |   |         | 2 |
| Isogeny                           |            |   |                | 1 |         | 1 |
| Total                             | 3          | 3 | 4              | 5 | 7       | 8 |

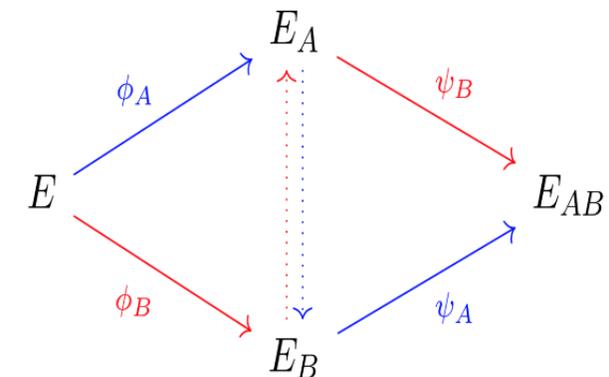
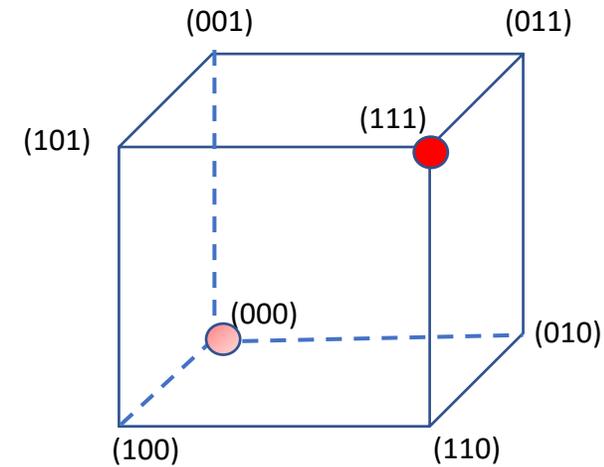
# Lattice-based KEMs

- Crystals-Kyber
  - Great all-around → Finalist
- Saber
  - Great all-around → Finalist
- NTRU
  - Not quite as efficient, but older, IP situation → Finalist
- NTRUprime
  - Different design choice and security model → Alternate
- FrodoKEM
  - Conservative/Backup → Alternate



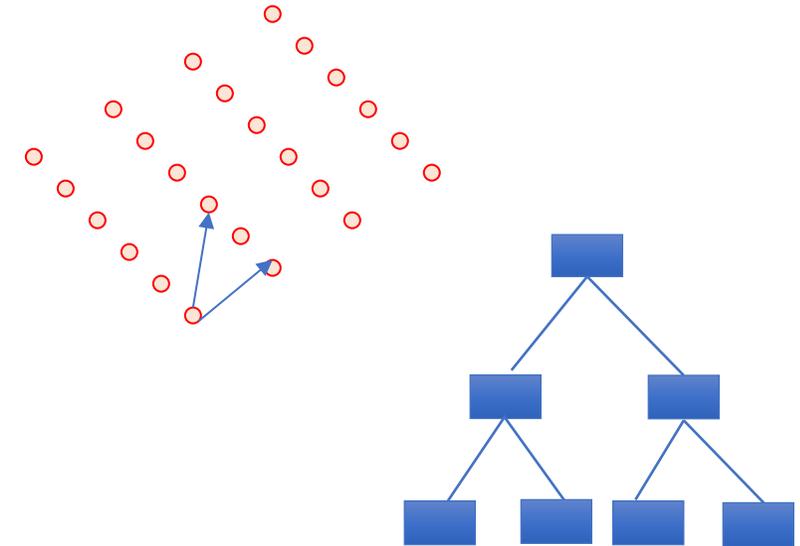
# Isogeny- and Code-based KEMs

- **Classic McEliece**
  - Oldest submission, large public keys but small ciphertexts → **Finalist**
- **BIKE**
  - Good performance, CCA security?, more time to be stable → **Alternate**
- **HQC**
  - Better security analysis/larger keys (than BIKE) → **Alternate**
- **SIKE**
  - Newer security problem, an order slower → **Alternate**



# The Signatures

- **Dilithium and Falcon**
  - Both balanced, efficient lattice-based signatures
  - coreSVP security higher?
  - → **Finalists**
- **SPHINCS+ and Picnic**
  - SPHINCS+ is stable, conservative security, larger/slower → **Alternate**
  - Picnic not stable yet, but has lots of potential → **Alternate**
- **Rainbow and GeMMS**
  - Both have large public keys, small signatures.  
Rainbow a bit better → **Finalist**, GeMMS → **Alternate**



$$\begin{aligned} p^{(1)}(x_1, \dots, x_n) &= \sum_{i=1}^n \sum_{j=i}^n p_{ij}^{(1)} \cdot x_i x_j + \sum_{i=1}^n p_i^{(1)} \cdot x_i + p_0^{(1)} \\ p^{(2)}(x_1, \dots, x_n) &= \sum_{i=1}^n \sum_{j=i}^n p_{ij}^{(2)} \cdot x_i x_j + \sum_{i=1}^n p_i^{(2)} \cdot x_i + p_0^{(2)} \\ &\vdots \\ p^{(m)}(x_1, \dots, x_n) &= \sum_{i=1}^n \sum_{j=i}^n p_{ij}^{(m)} \cdot x_i x_j + \sum_{i=1}^n p_i^{(m)} \cdot x_i + p_0^{(m)} \end{aligned}$$

- The 3<sup>rd</sup> round will last 12-18 months
  - NIST will then select which finalist algorithms to standardize
  - NIST will also select which alternates to keep studying in a 4<sup>th</sup> round (\*)
  - The 4<sup>th</sup> round will similarly be 12-18 months
  - NIST may decide to consider new schemes – details to come
- NIST will hold a 3rd PQC Standardization workshop ~ spring 2021
- We expect to release draft standards for public comment in 2022-2023
- The finalized standard will hopefully be ready by 2024

- Many important topics to be studied:
  - Security proofs in both the ROM and QROM
  - Does the specific ring/module/field choice matter for security?
    - Or choice of noise distribution?
    - Does “product” or “quotient” style LWE matter?
  - Finer-grained metrics for security of lattice-based crypto (coreSVP vs. real-world security)
  - Are there any important attack avenues that have gone unnoticed?
  - Side-channel attacks/resistant implementations for finalists and alternates
  - More hardware implementations
  - Ease of implementations – decryption failures, floating point arithmetic, noise sampling, etc.
- Specific algorithm questions
  - Decoding analysis for BIKE, category 1 security levels for Kyber/Saber/Dilithium, algebraic cryptanalysis of cyclotomics for lattices, etc...

- Many other challenges to work on
  - IP issues
  - Continued performance benchmarking in different platforms and environments
    - For hardware – NIST suggested Artix-7 and Cortex M4 (with all options) for easier comparison
  - Real world experiments
    - How do these algorithms work in actual protocols and applications.
      - Are some key sizes too large?

## Stateful hash-based signatures were proposed in 1970s

- Rely on assumptions on hash functions, that is, not on number theory complexity assumptions
- It is essentially limited-time signatures, which require state management

## NIST specification on stateful hash-based signatures

- NIST SP 800-208 *“Recommendation for Stateful Hash-Based Signature Schemes”*

## Internet Engineering Task Force (IETF) has released two RFCs on hash-based signatures

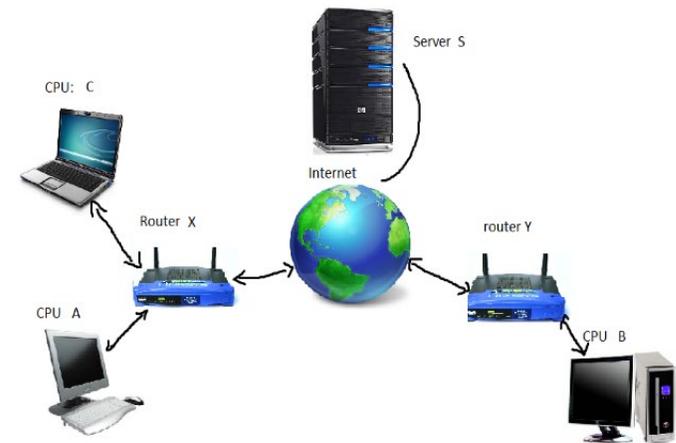
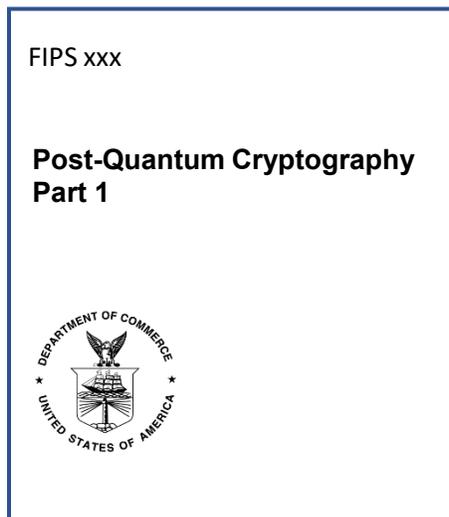
- [RFC 8391](#) “XMSS: eXtended Merkle Signature Scheme” (By Internet Research Task Force (IRTF))
- [RFC 8554](#) “Leighton-Micali Hash-Based Signatures” (By Internet Research Task Force (IRTF))

## ISO/IEC JTC 1 SC27 WG2 Project on hash-based signatures

- Stateful hash-based signatures will be specified in ISO/IEC 14888 Part 4
- It is in the 1st Working Draft stage

# Transition and Migration

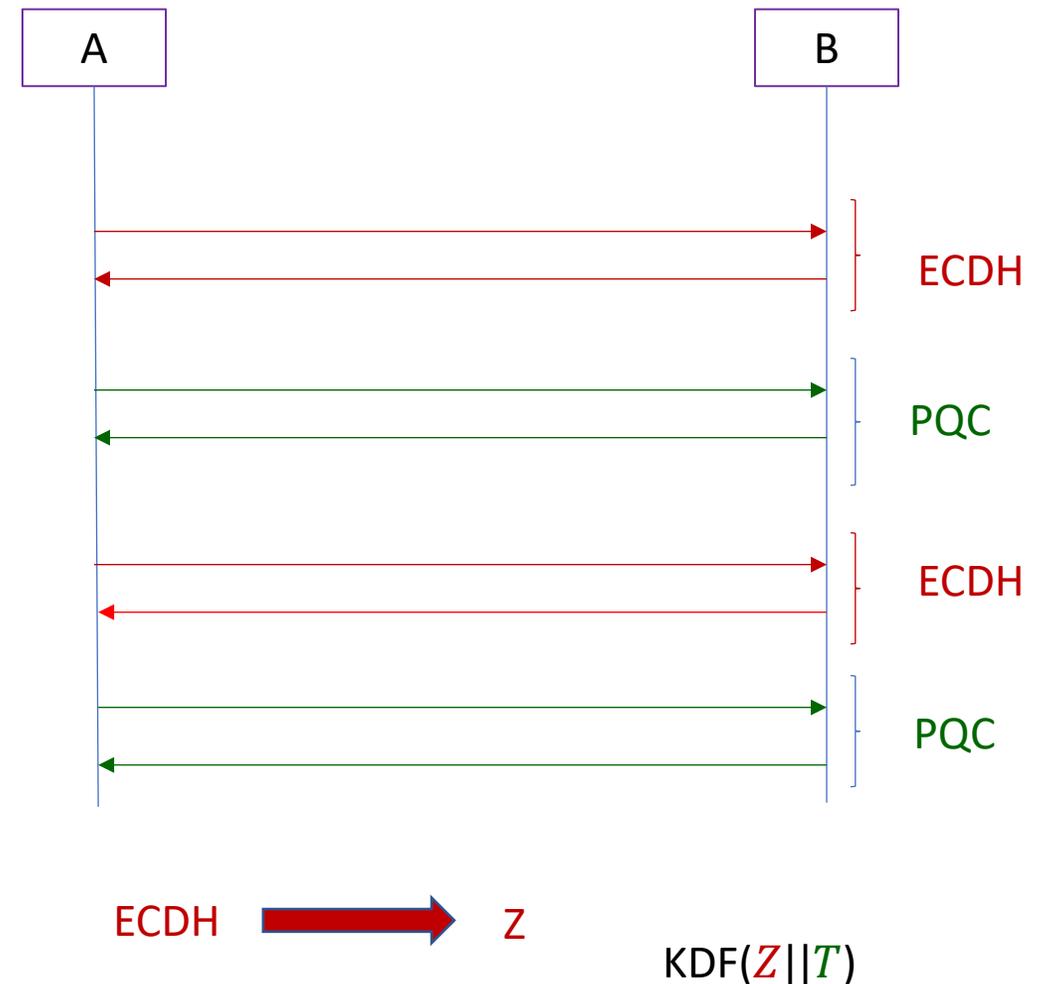
- Public key Cryptography has been used everywhere; 2 important uses:
  - Communication security; and
  - Trusted platforms
- Transition and migration are going to be a long journey full of exciting adventures
  - Understand new features, characters, implementation challenges
  - Identify barriers, issues, show-stoppers, needed justifications, etc.
  - Reduce the risk of disruptions in operation and security



# Hybrid mode – An approach for migration

## NIST SP800-56C Rev. 2 *Recommendation for Key-Derivation Methods in Key-Establishment Schemes* August 2020

“In addition to the currently approved techniques for the generation of the shared secret  $Z$  ... this Recommendation permits the use of a “hybrid” shared secret of the form  $Z' = Z || T$ , a concatenation consisting of a “standard” shared secret  $Z$  that was generated during the execution of a key-establishment scheme (as currently specified in [SP 800-56A] or [SP 800-56B]) followed by an auxiliary shared secret  $T$  that has been generated using some other method”



# NIST Transition Guideline for PQC?



NIST has published transition guidelines for algorithms and key lengths

## NIST SP 800-131A Revision 2 “Transitioning the Use of Cryptographic Algorithms and Key Lengths” - Examples

- Three-key Triple DES
  - Encryption - Deprecated through 2023 Disallowed after 2023
  - Decryption - Legacy use
- SHA-1
  - Digital signature generation - Disallowed, except where specifically allowed by NIST protocol-specific guidance
  - Digital signature verification - Legacy use
  - Non-digital signature applications – Acceptable
- Key establishment methods with strength  $< 112$  bits (e.g. DH mod  $p$ ,  $|p| < 2048$ )
  - Disallowed

NIST will provide transition guidelines to PQC standards

- The timeframe will be based on a risk assessment of quantum attacks
- NCCoE hosted a workshop on [Considerations in Migrating to Post-Quantum Cryptographic Algorithms](#) on October 7

# What can organizations do now?

- **Perform a quantum risk assessment within your organization**
  - Identify information assets and their current crypto protection
  - Identify what 'x', 'y', and 'z' might be for you – determine your quantum risk
  - Prioritize activities required to maintain awareness, and to migrate technology to quantum-safe solutions
- **Evaluate vendor products with quantum safe features**
  - Know which products are not quantum safe
  - Ask vendors for quantum safe features in procurement templates
- **Develop an internal knowledge base amongst IT staff**
- **Track developments in quantum computing and quantum safe solutions, and to establish a roadmap to quantum readiness for your organization**
- **Act now – it will be less expensive, less disruptive, and less likely to have mistakes caused by rushing and scrambling**

# Conclusion

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- We can start to see the end?
- NIST is grateful for everybody's efforts
- Check out [www.nist.gov/pqcrypto](https://www.nist.gov/pqcrypto)
  - Sign up for the pqc-forum for announcements & discussion
  - send e-mail to [pqc-comments@nist.gov](mailto:pqc-comments@nist.gov)